

ECE-205

Exam 3

Fall 2012

Calculators and computers are not allowed. You must show your work to receive credit.

Problem 1 _____/20

Problem 2 _____/15

Problem 3 _____/15

Problem 4 _____/20

Problems 5 _____/30

Total _____

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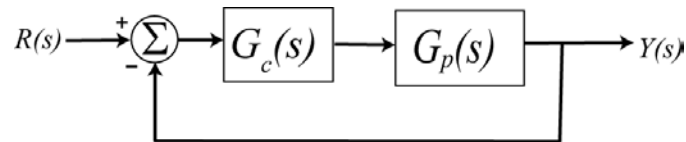
1) (20 points) For the following transfer functions, determine the unit step response of the system. *Do not forget any necessary unit step functions.*

a) $H(s) = \frac{e^{-2s}}{s}$

b) $H(s) = \frac{1}{(s+1)^2}$

c) $H(s) = \frac{1}{s^2 + 2s + 5}$

2) (15 points) Consider the following simple feedback control block diagram. The plant, the thing we want to control, has the transfer function $G_p(s) = \frac{5}{s+3}$



- a) Determine the settling time of the plant alone (assuming there is no feedback)

- b) Determine the steady state error for plant alone assuming the input is a unit step (simplify your answer)

- c) For a proportional controller, $G_c(s) = k_p$, determine the closed loop transfer function $G_0(s)$

- d) Determine the settling time of the closed loop system, in terms of k_p

- e) Determine the steady state error of the closed loop system for a unit step, in terms of k_p (simplify your answer)

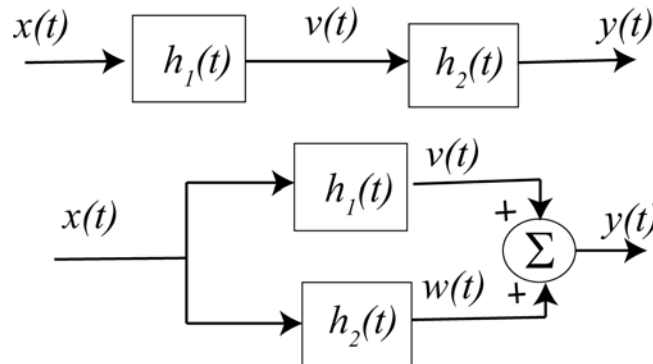
- f) For an integral controller, $G_c(s) = \frac{k_i}{s}$, determine the closed loop transfer function $G_0(s)$ and the steady state error for a unit step in terms of k_i

3) (15 points) For the following block diagram

For the following interconnected systems,

i) determine the overall impulse response (the impulse response between input $x(t)$ and output $y(t)$) and

ii) determine if the system is causal.



a) $h_1(t) = \delta(t-2)$, $h_2(t) = \delta(t+1)$

b) $h_1(t) = u(t+1)$, $h_2(t) = u(t-2) + \delta(t-2)$

Series Connections:

Parallel Connections:

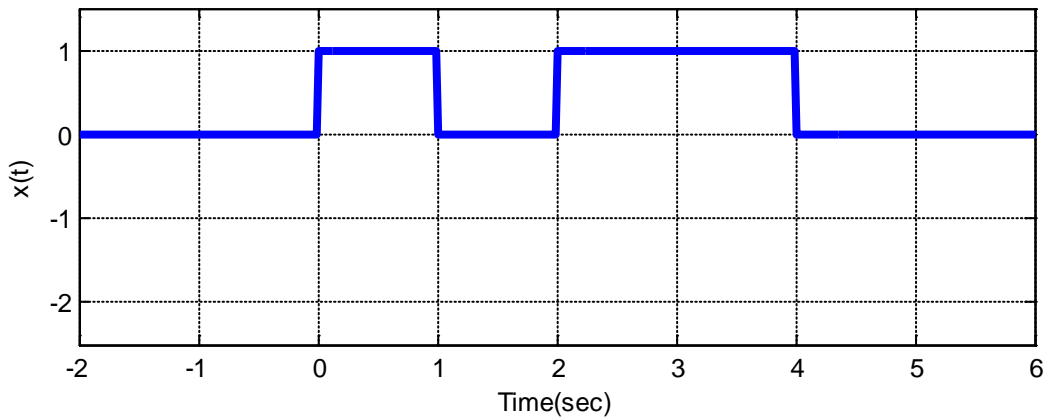
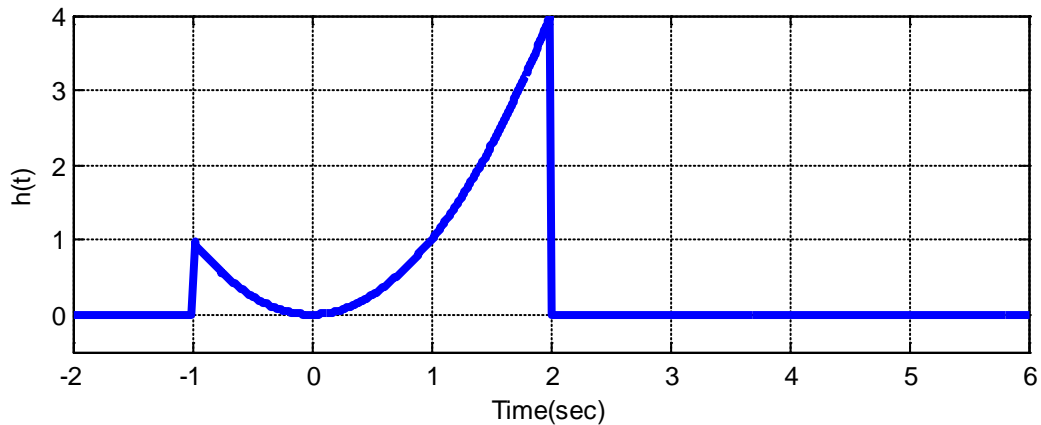
4) (20 points) Consider a linear time invariant system with impulse response given by

$$h(t) = t^2[u(t+1) - u(t-2)]$$

The input to the system is given by

$$x(t) = [u(t) - u(t-1)] + [u(t-2) - u(t-4)]$$

The impulse response and input are shown below:



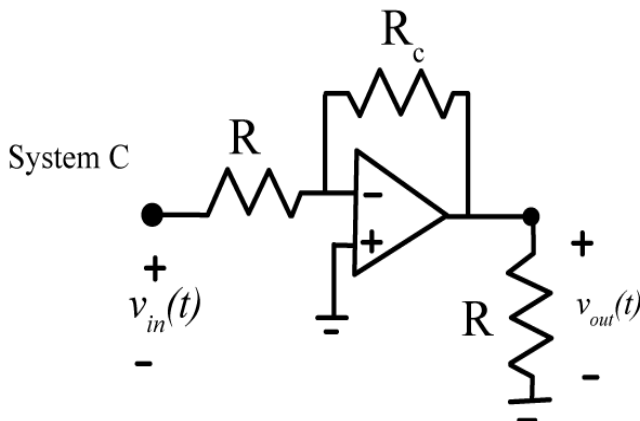
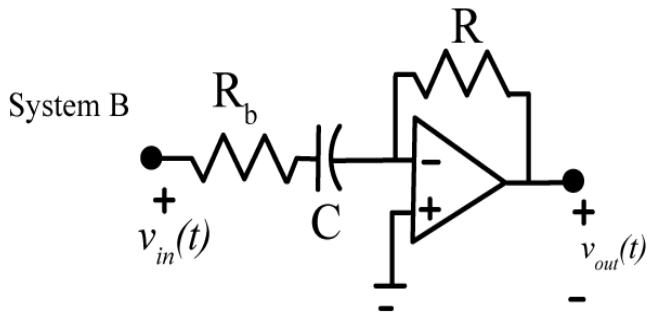
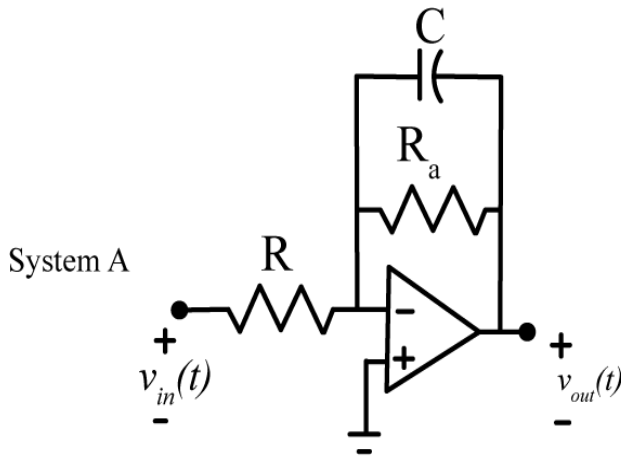
Using graphical evaluation, determine the output $y(t)$. Specifically, you must

- Flip and slide $h(t)$, **NOT** $x(t)$
- Show graphs displaying both $h(t - \lambda)$ and $x(\lambda)$ for each region of interest
- Determine the range of t for which each part of your solution is valid
- Set up any necessary integrals to compute $y(t)$. Your integrals must be complete, in that they cannot contain the symbols $x(\lambda)$ or $h(t - \lambda)$ but must contain the actual functions.
- Your integrals cannot contain any unit step functions
- **DO NOT EVALUATE THE INTEGRALS!!**

5) (30 points) The following figure shows three different circuits, which are subsystems for a larger system. We can write the transfer functions for these systems as

$$G_a(s) = \frac{-K_{low}\omega_{low}}{s + \omega_{low}} \quad G_b(s) = \frac{-K_{high}s}{s + \omega_{high}} \quad G_c(s) = -K_{ap}$$

Determine the parameters K_{low} , ω_{low} , K_{high} , ω_{high} , and K_{ap} in terms of the parameters given (the resistors and capacitors).



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