

# **ECE-205**

## **Exam 3**

### **Fall 2011**

**Calculators and computers are not allowed. You must show your work to receive credit.**

**Problem 1 \_\_\_\_\_/30**

**Problem 2 \_\_\_\_\_/15**

**Problem 3 \_\_\_\_\_/20**

**Problem 4 \_\_\_\_\_/15**

**Problems 5 \_\_\_\_\_/20**

**Total \_\_\_\_\_**

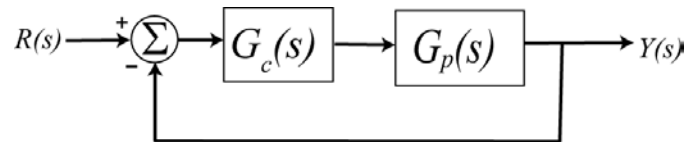
1) (30 points) For the following transfer functions, determine **both** the impulse response and the unit step response of the system. *Do not forget any necessary unit step functions.*

a)  $H(s) = \frac{e^{-s}}{(s+2)}$

b)  $H(s) = \frac{1}{(s+1)^2}$

c)  $H(s) = \frac{s}{s^2 + 4s + 5}$

**2) (15 points)** Consider the following simple feedback control block diagram. The plant, the thing we want to control, has the transfer function  $G_p(s) = \frac{3}{s+5}$



- a)** Determine the settling time of the plant alone (assuming there is no feedback)
- b)** Determine the steady state error for plant alone assuming the input is a unit step (simplify your answer)
- c)** For a proportional controller,  $G_c(s) = k_p$ , determine the closed loop transfer function  $G_0(s)$
- d)** Determine the settling time of the closed loop system, in terms of  $k_p$
- e)** Determine the steady state error of the closed loop system for a unit step, in terms of  $k_p$  (simplify your answer)
- f)** For an integral controller,  $G_c(s) = \frac{k_i}{s}$ , determine the closed loop transfer function  $G_0(s)$  and the steady state error for a unit step in terms of  $k_i$

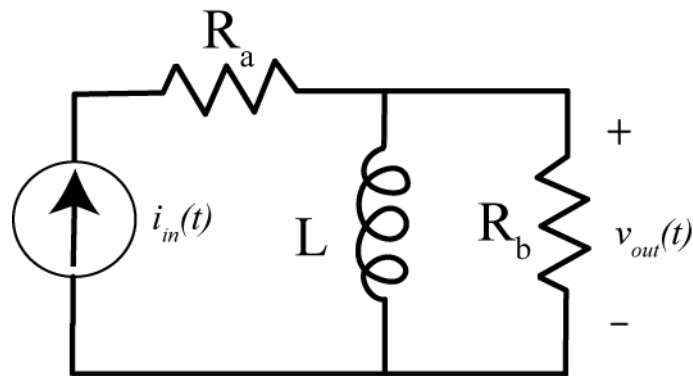
3) (20 points) For the following circuit determine

a) the zero input response (ZIR)

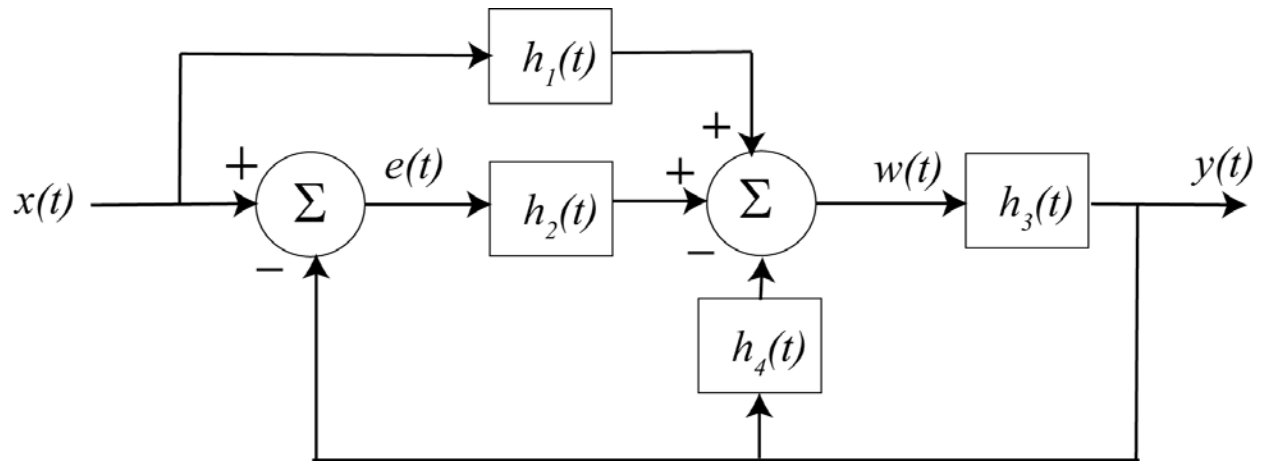
b) the zero state response (ZSR)

c) the transfer function  $H(s)$

*Note; You will need to include initial conditions for some of this problem.*



4) (15 points) For the following block diagram



Draw the corresponding signal flow graph, labeling each branch and direction. *Feel free to insert as many branches with a gain of 1 as you think you may need.*

Determine the system transfer function using Mason's gain rule. *You must clearly indicate all of the paths, the loops, the determinant and the cofactors. **You need to simplify your final answer!***

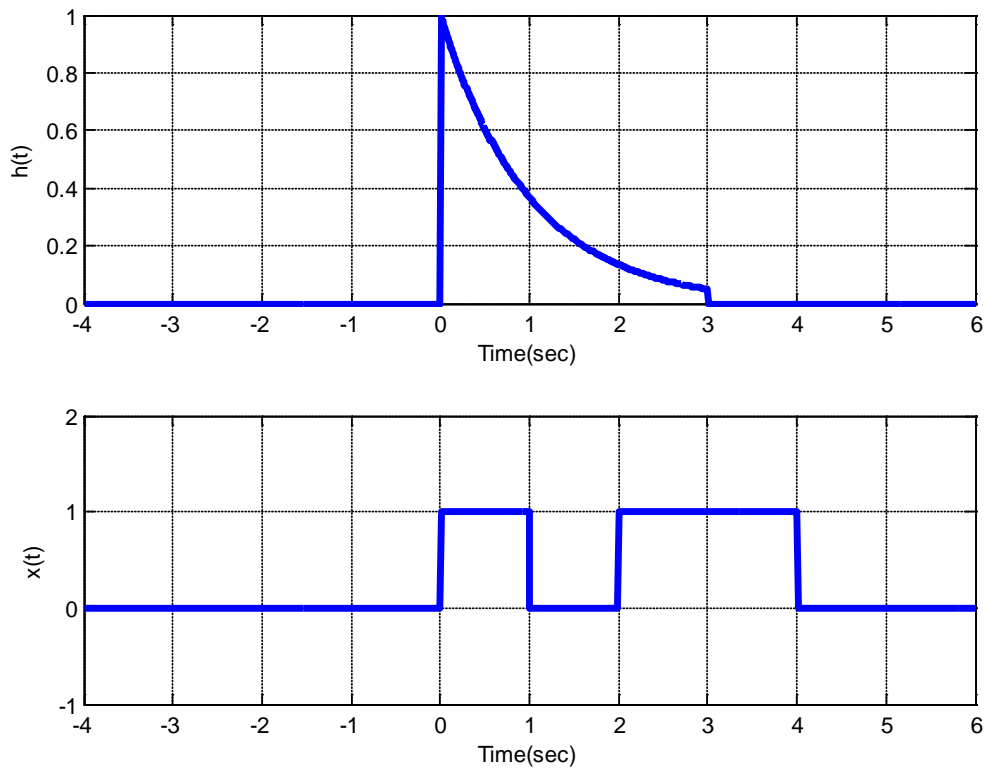
5) (20 points) Consider a linear time invariant system with impulse response given by

$$h(t) = e^{-t}[u(t) - u(t - 3)]$$

The input to the system is given by

$$x(t) = [u(t) - u(t - 1)] + [u(t - 2) - u(t - 4)]$$

The impulse response and input are shown below:



Using **graphical evaluation**, determine the output  $y(t)$ . Specifically, you must

- Flip and slide  $h(t)$ , **NOT**  $x(t)$
- Show graphs displaying both  $h(t - \lambda)$  and  $x(\lambda)$  for each region of interest
- Determine the range of  $t$  for which each part of your solution is valid
- Set up any necessary integrals to compute  $y(t)$ . Your integrals must be complete, in that they cannot contain the symbols  $x(\lambda)$  or  $h(t - \lambda)$  but must contain the actual functions.
- Your integrals cannot contain any unit step functions
- **DO NOT EVALUATE THE INTEGRALS!!**

Name \_\_\_\_\_ Mailbox \_\_\_\_\_

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