## ECE-205 Exam 3 Fall 2010

Calculators and computers are not allowed. You must show your work to receive credit.

Problem 1	/30
Problem 2	/20
Problem 3	/20
Problem 4	/21
Problems 5-7	/9
Total	

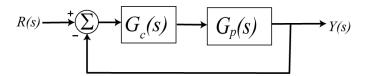
1) (30 points) For the following transfer functions, determine the <u>unit step response</u> of the system. *Do not forget any necessary unit step functions*.

a) 
$$H(s) = \frac{e^{-2s}}{(s+1)(s+2)}$$

b) 
$$H(s) = \frac{1}{(s+2)^2}$$

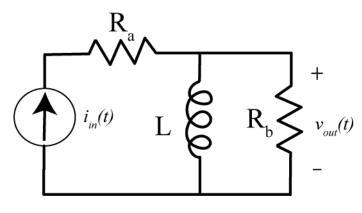
c) 
$$H(s) = \frac{5}{s^2 + 4s + 5}$$

2) (20 points) Consider the following simple feedback control block diagram. The plant, the thing we want to control, has the transfer function  $G_p(s) = \frac{4}{s+3}$ 



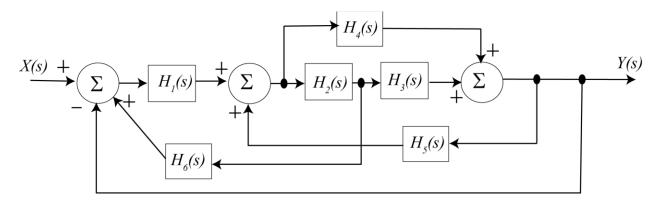
- a) Determine the settling time of the plant alone (assuming there is no feedback)
- **b)** For a proportional controller,  $G_c(s) = k_p$ , determine the closed loop transfer function  $G_0(s)$  and then
  - i) the settling time, in terms of  $k_p$
  - ii) the steady state error for a unit step, in terms of  $k_p$
- c) For and integral controller,  $G_c(s) = \frac{k_i}{s}$ , determine the closed loop transfer function  $G_0(s)$  and the steady state error for a unit step in terms of  $k_i$

**3)** (**20 points**) For the following circuit determine the <u>transfer function</u> and the corresponding <u>impulse response</u>.



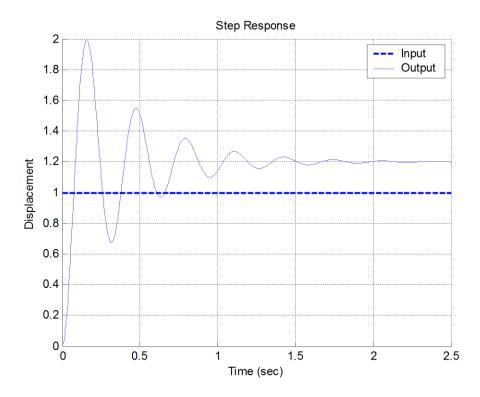
.

4) (20 points) For the following block diagram



- **a)** Draw the corresponding signal flow graph, labeling each branch and direction. *Feel free to insert as many branches with a gain of 1 as you think you may need.*
- **b)** Determine the system transfer function using Mason's gain rule. You must clearly indicate all of the paths, the loops, the determinant and the cofactors, but you do not need to simplify your final answer (it can be written in terms of the  $P_i, L_i$ , and  $\Delta_i$ )

Problems 5-6 refer to the **unit step response** of a system, shown below



- 5) (3 points) The best estimate of the steady state error for a unit step input is
- a) 0.20 b) -0.20 c) 1.0 d) -0.0
- 6) (3 points) The best estimate of the percent overshoot is
- a) 200% b) 100% c) 67% d) 20%
- 7) (3 points) How many of the following transfer functions represents (asymptotically) stable systems?

$$G_a(s) = \frac{s-1}{s+1}$$

$$G_b(s) = \frac{1}{s(s+1)}$$

$$G_c(s) = \frac{s}{s^2 - 1}$$

$$G_d(s) = \frac{s+1}{(s+1+j)(s+1-j)}$$

$$G_e(s) = \frac{(s-1-j)(s-1+j)}{s}$$

$$G_a(s) = \frac{s-1}{s+1} \qquad G_b(s) = \frac{1}{s(s+1)} \qquad G_c(s) = \frac{s}{s^2 - 1}$$

$$G_d(s) = \frac{s+1}{(s+1+j)(s+1-j)} \qquad G_e(s) = \frac{(s-1-j)(s-1+j)}{s} \qquad G_f(s) = \frac{(s-1-j)(s-1+j)}{(s+1-j)(s+1+j)}$$

a) 0 b) 1 c) 1 d) 3 e) 4 f) 5 g) 6

Name	Mailbox

Name	Mailbox