ECE 130 HW\#6 - Due Thursday, March 25

1. Consider the following truth table where the four-bit number $\mathrm{A}(\mathrm{A} 3, \mathrm{~A} 2, \mathrm{~A} 1, \mathrm{~A} 0)$ is input and X is output:

| $\mathbf{A 3}$ | $\mathbf{A 2}$ | $\mathbf{A 1}$ | $\mathbf{A} \mathbf{0}$ | $\mathbf{X}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 1 |
| 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 |

a. Convert the truth table into a K-Map.

b. Use the K-Map to develop a minimized slm-of-products equation for the output X.
from red: $\mathrm{X}=\mathrm{A} 3^{*} \mathrm{~A}^{\prime}{ }^{\prime}+\mathrm{A} 2^{\prime} * \mathrm{~A} 1+\mathrm{A} 3^{*} \mathrm{~A} 1^{*} \mathrm{~A} 0^{\prime}+\mathrm{A} 2^{\prime} * \mathrm{~A} 0^{\prime}$
c. Use the K-Map to develop a minimized product-of-sums equation for the output X .
from green: $\mathrm{X}=\left(\mathrm{A} 2^{\prime}+\mathrm{A} 1\right)\left(\mathrm{A} 2^{\prime}+\mathrm{A} 0^{\prime}\right)\left(\mathrm{A} 3+\mathrm{A} 2^{\prime}\right)\left(\mathrm{A} 3+\mathrm{A} 1+\mathrm{A} 0^{\prime}\right)$
d. State the number of inputs used for each of the two equations. Based on these numbers, which equation is more efficient? Why?

SoP: 13 inputs
PoS: 13 inputs. Go with PoS since both expressions have same number of inputs.
e. Implement the more efficient equation using either NAND-NAND or NOR-NOR two level logic. Draw your circuit below. You can use the complemented and uncomplemented forms of all of the variables.


