

## ECE250 Equation Sheet Test 1 April 1, 2010 (KEH)

**Diode Equation:**  $I_d = I_s \cdot (e^{V_d/(nV_T)} - 1)$  where  $I_s$  = reverse saturation current.  $I_s$  **DOUBLES** for every 10 degree C rise  
 $V_d$  is the anode-to-cathode voltage and  $I_d$  is current flowing into anode

**Thermal Voltage:**  $V_T = kT/q = 25.7$  mV at room temperature  $T = 300$ K.

**DC load voltage:**  $V_{dc} = V_{m,s} - 0.7V - V_r / 2$  (half-wave rect)  $V_{dc} = V_{m,s} - 1.4V - V_r / 2$  (full-wave rect)

**Half-wave rectifier ripple voltage:**  $V_r = \frac{(V_{m,s} - 0.7V - V_r / 2) / R_L}{f_{source} \cdot C}$   $V_{m,s}$  = peak source voltage

**Full-wave diode bridge rectifier ripple voltage:**  $V_r = \frac{(V_{m,s} - 1.4V - V_r / 2) / R_L}{2f_{source} \cdot C}$   $V_{m,s}$  = peak source voltage

**Full-wave diode bridge peak diode current:**  $I_{d\max} = \frac{V_m}{R_L} \cdot (1 + 2\pi) \cdot \sqrt{\frac{V_m}{2 \cdot V_r}}$ , where  $V_m = V_{m,s} - 2(0.7V)$

**Small-Signal ac Model of Diode:**  $r_d = \frac{n \cdot V_T}{I_{dQ}}$ , where  $I_{dQ}$  is the dc (quiescent) component of the diode current.

**Plotting Load Lines over nonlinear element's IV curve:** First find Thevenin equivalent "looking out" from the terminals of the nonlinear element. Then plot load line:  $I_{\text{INTERCEPT}} = V_{th}/R_{th}$ , and  $V_{\text{INTERCEPT}} = V_{th}$

**Multiple Diode Analysis using 0.7 V battery model of diode:** Define  $I_d$ 's flowing into each anode. Define  $V_d$ 's anode-to-cathode. Guess which diodes are ON and replace them with 0.7 battery, replace OFF diodes with open circuit. Analyze circuit. Check to ensure diodes that are assumed ON have  $I_d > 0$ , and diodes that are assumed OFF have  $V_d < 0.7$  V.

**Carrier Concentration in Intrinsic Si ( $1/\text{cm}^3$ ):**  $n_i^2 = BT^3 e^{-E_g/kT}$

at  $T=300$ K:  $B=5.4 \times 10^{31}/(\text{K}^3 \text{cm}^6)$ ,  $E_g=1.12$  eV,  $k=$  Boltzmann's Constant  $= 8.62 \times 10^{-5}$  eV/K,  $n_i=1.5 \times 10^{10}$   $1/\text{cm}^3$

**Diffusion Current Density ( $\text{A}/\text{cm}^2$ ):**  $J_p = -qD_p \frac{dp}{dx}$   $J_n = qD_n \frac{dn}{dx}$   $q = 1.6 \times 10^{-19}$  Coulombs  
 $D_p = 12$   $\text{cm}^2/\text{s}$ ,  $D_n = 34$   $\text{cm}^2/\text{s}$

**Drift current Density ( $\text{A}/\text{cm}^2$ ):**  $J_{\text{drift}} = q(p\mu_p + n\mu_n)E$

**Resistivity ( $\Omega\text{-cm}$ ) and Resistance ( $\Omega$ ):**  $\rho = 1/[q(p\mu_p + n\mu_n)]$   $R = \rho L/A$

**Carrier Concentration in n-type Si ( $1/\text{cm}^3$ ):**  $n_{n0} = N_D$  **in p-type Si ( $1/\text{cm}^3$ ):**  $p_{p0} = N_A$   
 $p_{n0} = n_i^2 / N_D$   $n_{p0} = n_i^2 / N_A$

**Built-In Junction Voltage (V):**  $V_0 = V_T \ln\left(\frac{N_A N_D}{n_i^2}\right)$

**Depletion Region Capacitance (F):**  $C_j = \frac{C_{j0}}{\left(1 + \frac{V_R}{V_0}\right)^m}$  **where**  $C_{j0} = \epsilon_{\text{Si}} A / (W_{\text{depletion\_region}})_{V_R=0}$

and  $m =$  junction grading coefficient  $= 1/3$  to  $1/2$ ,

also note  $V_R$  is diode's CATHODE to ANODE voltage  $= -V_d$