DTTF/NB479: Dszquphsbqiz

Day 7

Announcements:

- Matlab tutorial linked to in syllabus
- Questions?
- Today:
 - Substitution ciphers
 - Matrix inverses
 - Hill ciphers

Block Ciphers

- So far, changing 1 character in the plaintext changes
 ___ character(s) in the ciphertext.
- Shannon outlined qualities of good ciphers:
 - Diffusion: Changing one character of the plaintext changes
 ____ characters in the ciphertext
 - Makes frequency analysis much tougher!
 - Confusion: Each character of the ciphertext interacts with several parts of the key
- Block ciphers have both qualities:
 - DES (64 bits), AES (128 bits), Hill ciphers (smaller; today)

Hill Ciphers

- Lester Hill, 1929. Not used much, but is historically significant: first time linear algebra used in crypto
- Use an n x n matrix M. Encrypt by breaking plaintext into blocks of length n (padding with x's if needed) and multiplying each by M (mod 26).
- Example: Encrypt "hereissomeonetoencrypt" using M
- her eis som eon eto enc ryp txx
- (7, 4, 17) (4, 8, 18) ... (19, 23, 23)

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 11 & 9 & 8 \end{bmatrix}$$

- (0, 22, 15)
- cfz acw yga vns ave anc sdd awp
- "CFZACWYGAVNSAVEANCSDDAWP"

Decrypting

• Reverse the process, multiplying each block by M inverse (mod n)

- Theorem: If a matrix M is invertible mod n, then gcd(det(M), n) = 1
- Proof on board

Modular matrix inverse (§3.8)

The Hill cipher requires us to invert a matrix mod
 26.

- For a 2x2 matrix, this is easy.
- Many numerical packages allow us to invert a matrix, but using floating point numbers.

- How do we combine the two?
 - Demo of my code

How to break via known plaintext?

• Answering Q7 preps you to do 2.13 #14 on HW2 if you want to earn an early day

You may leave when done