



**FIGURE 1.6** A black box optimization problem with five on-off switches illustrates the idea of a coding and a payoff measure. Genetic algorithms only require these two things: they don't need to know the workings of the black box.

**TABLE 1.2 A Genetic Algorithm by Hand**

String No.	Initial Population (Randomly Generated)	$x$ Value (Unsigned Integer)	$f(x)$	$p_{select_i} = \frac{f_i}{\Sigma f}$	Expected count $\frac{f_i}{\bar{f}}$	Actual Count from Roulette Wheel
1	0 1 1 0 1	13	169	0.14	0.58	1
2	1 1 0 0 0	24	576	0.49	1.97	2
3	0 1 0 0 0	8	64	0.06	0.22	0
4	1 0 0 1 1	19	361	0.31	1.23	1
<b>Sum</b>			1170	1.00	4.00	4.0
<b>Average</b>			<u>293</u>	0.25	1.00	1.0
<b>Max</b>			<u>576</u>	0.49	1.97	2.0

**TABLE 1.2 (Continued)**

Mating Pool after Reproduction (Cross Site Shown)	Mate (Randomly Selected)	Crossover Site (Randomly Selected)	New Population	$x$ Value	$f(x)$
0 1 1 0   1	2	4	0 1 1 0 0	12	144
1 1 0 0   0	1	4	1 1 0 0 1	25	625
1 1   0 0 0	4	2	1 1 0 1 1	27	729
1 0   0 1 1	3	2	1 0 0 0 0	16	256
					1754
					<u>439</u>
					<u>729</u>

## Inversion:

Inside of a string, randomly select two cities and flip them around

A: 9 8 4 2 3 10 1 6 5 7

A': 9 1 4 2 3 10 8 6 5 7

PMX (Partially Matched Crossover):

A: 9 8 4 | 5 6 7 | 1 3 2 10

B: 8 7 1 | 2 3 10 | 9 5 4 6

exchange    2 <-> 5

              6 <-> 3

              7 <-> 10

resulting in:

A': 9 8 4 | 2 3 10 | 1 6 5 7

B': 8 10 1 | 5 6 7 | 9 2 4 3

## Greedy Mutation:

1. Pick two cities at random
2. Switch them, if the new tour is shorter than the old one.

Greedy Crossover (Grefenstette):

A: 9 8 4 5 6 7 1 3 2 10

B: 8 7 1 2 3 10 9 5 4 6

Create a child by doing the following:

- 1) Pick a start city at random
- 2) Look at successor cities in both parents
- 3) Pick the one with the lower distance
- 4) If the selected city creates a cycle, pick the one from the other parent
- 5) If the selected city creates a cycle, pick a non-selected city at random
- 6) Goto (2)