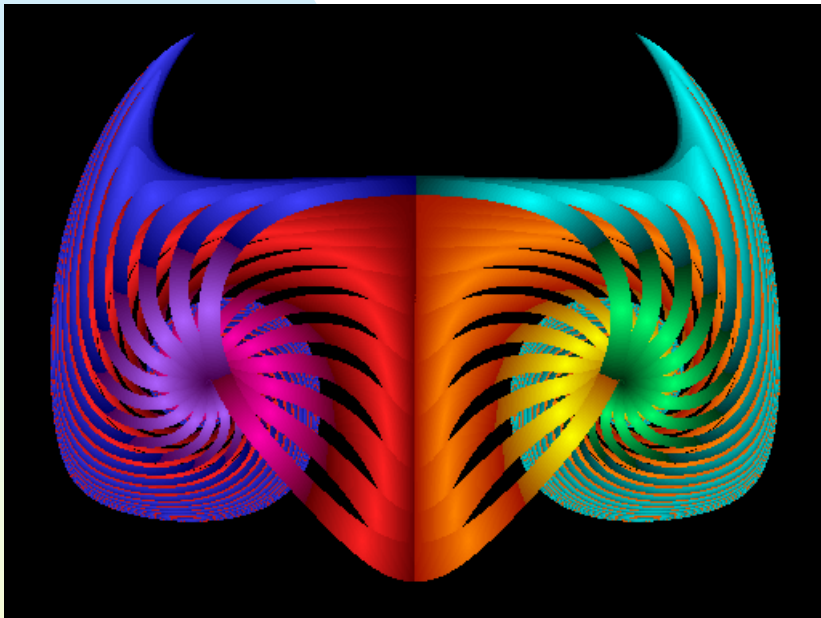
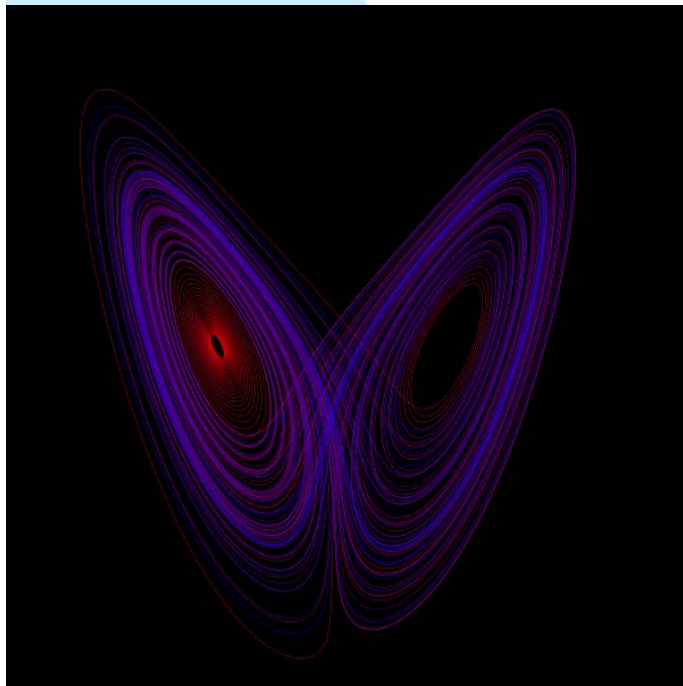


# Session overview



- Complex maps and Julia sets
- Reminder: project topics and teams due Thursday before class, earlier is better.
  - ◆ Submit survey on Angel

# Examples of Lyapunov Exponents

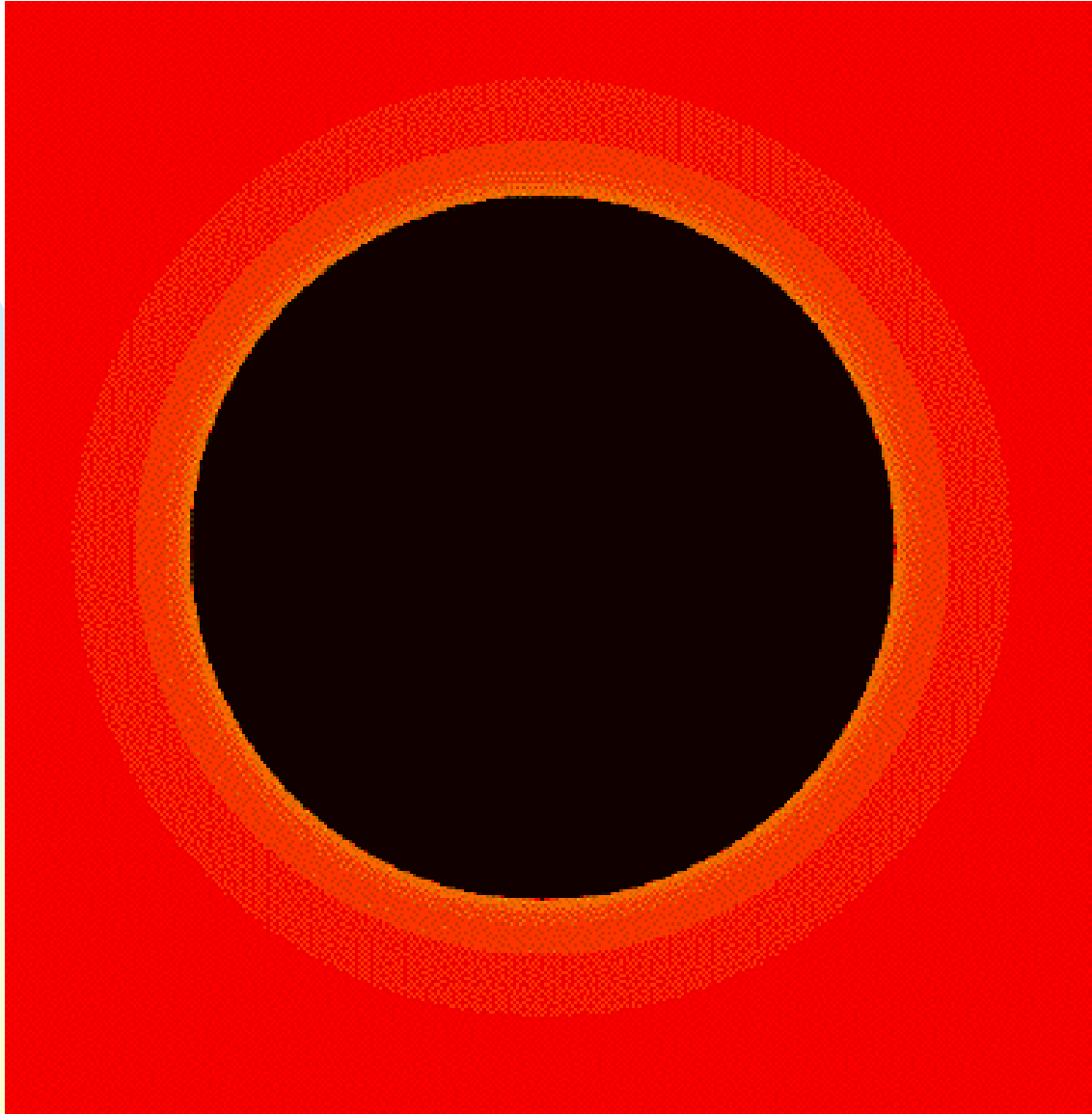


- Henon attractor:  $\lambda = 0.419217$
- Lorenz attractor:  $\lambda = 0.90563$  (for the parameters given earlier)
- Rossler attractor:  $\lambda = 0.13$  (for  $a=0.15$ ,  $b=0.2$ ,  $c=10$ )

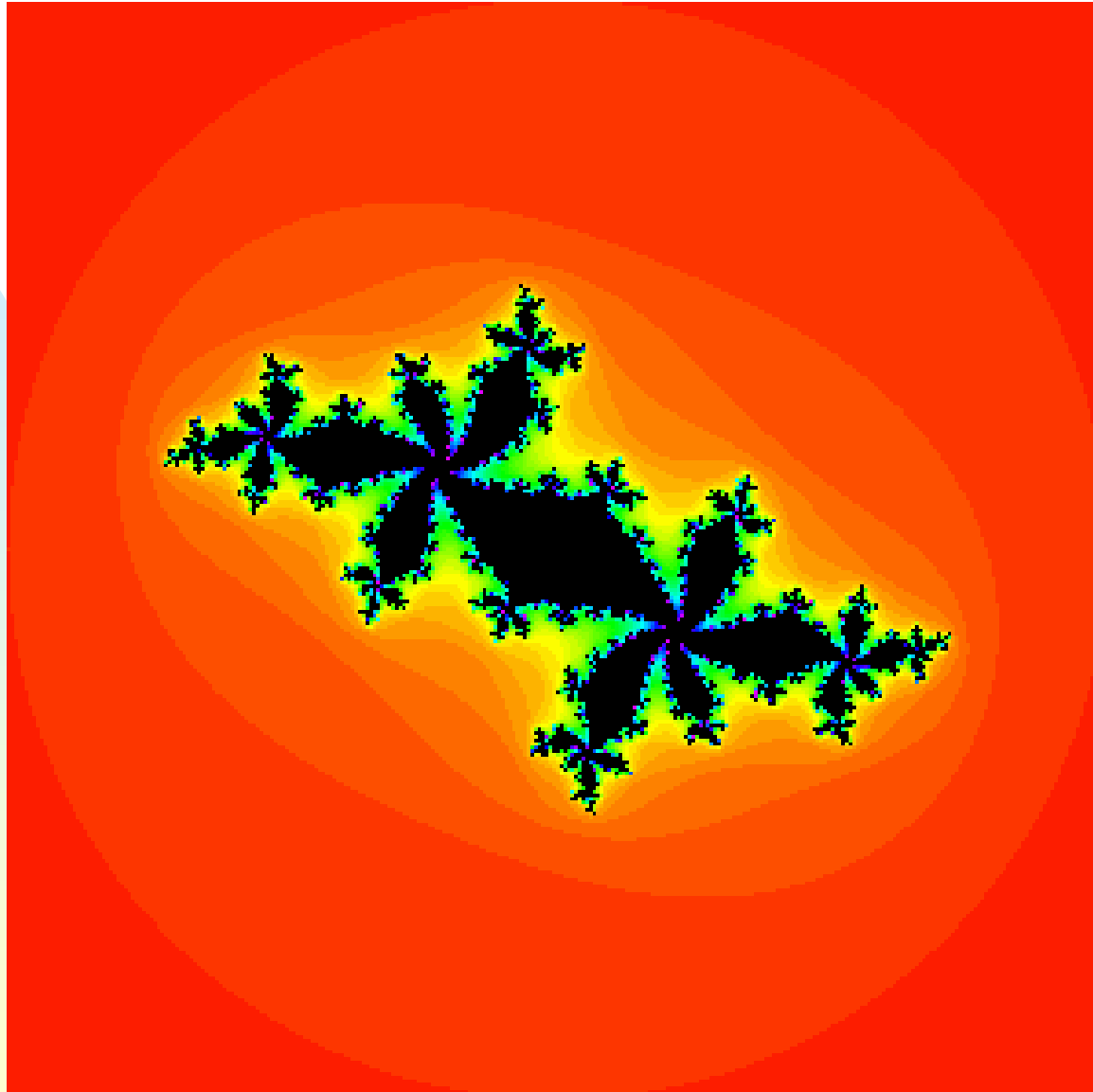
# Consider $f(z)=z^2$

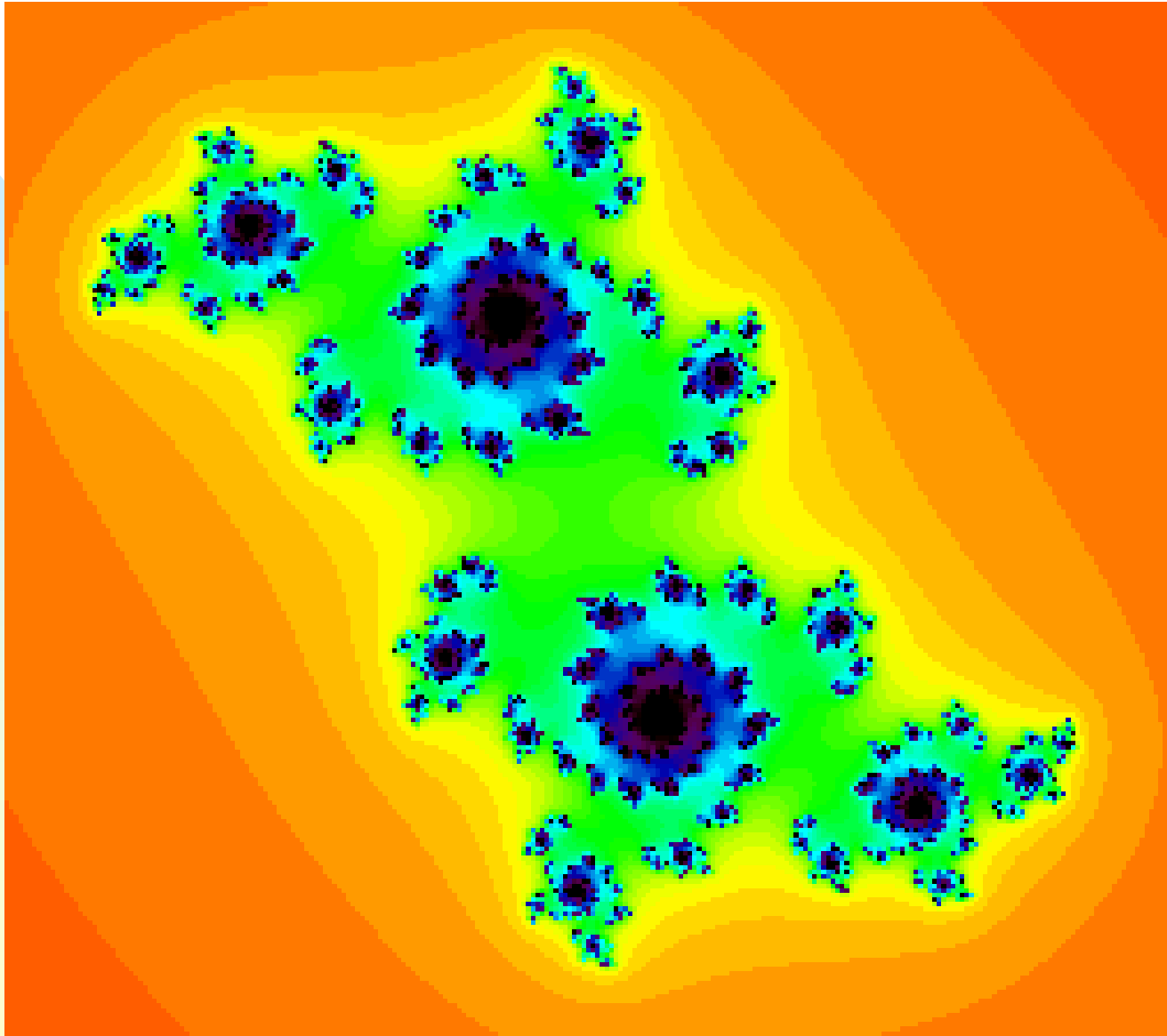
- Plot a number of points together
- Define the escape set and the prisoner set
- Define Julia set
- Define filled Julia set

$$c = 0$$



$$c = -0.52 + 0.57i$$





April 29, 2008

CSSE/MA 325 Lecture #27

6

# Inverse iteration

- Graphically, one of the easiest ways to find the Julia set is by the *inverse iteration* method
- In this method, we take successive square roots of  $z$  and plot them
- Use polar form for a complex number to take the square root
  - ◆ take the square root of the magnitude
  - ◆ take half the angle

# Square root properties

- Recognize that successive square roots approach 1 in magnitude
- A typical value for  $z_0$  is  $0.5 + 0.5i$
- There are two possible square roots at each stage:
  - ◆ angle is half the original angle
  - ◆ angle is  $\pi +$  half the original angle
- Choose either angle randomly



# Example program 1

- The inverse iteration method generates boundaries
- Program `juliasets.cpp` demonstrates this