

# CSSE 230 Day 28

Graphs and their representations

<https://www.google.com/maps/preview#!data=!1m4!1m3!1d989355!2d-87.4496039!3d38.8342589!4m26!3m17!1m5!1sRose-Hulman+Institute+of+Technology%2C+5500+Wabash+Ave%2C+Terre+Haute%2C+IN+47803!2s0x886d6e421b703737%3A0x96447680305ae1a4!3m2!3d39.482156!4d-87.322345!1m1!1sHoliday+World+%26+Splashin'+Safari%2C+Santa+Claus%2C+IN!3m8!1m3!1d245622!2d-86.923997!3d39.3256455!3m2!1i1920!2i955!4f13.1!5m2!13m1!1e1!7m4!11m3!1m1!1e1!2b1&fid=0>

# Graphs

Terminology

Representations

Algorithms

# Example Graph

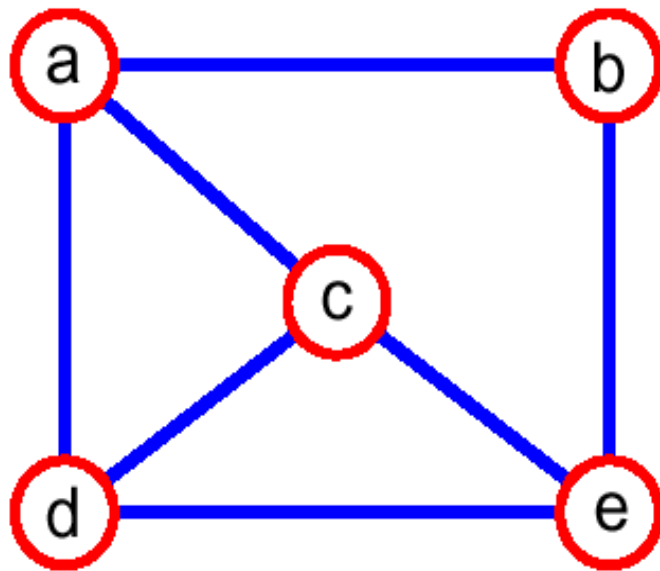
A graph  $G = (V, E)$  is composed of:

$V$ : set of *vertices*

$E$ : set of *edges* connecting the *vertices* in  $V$

An **edge**  $e = (u, v)$  is a pair of *vertices*

Example:



$V = \{a, b, c, d, e\}$

$E =$

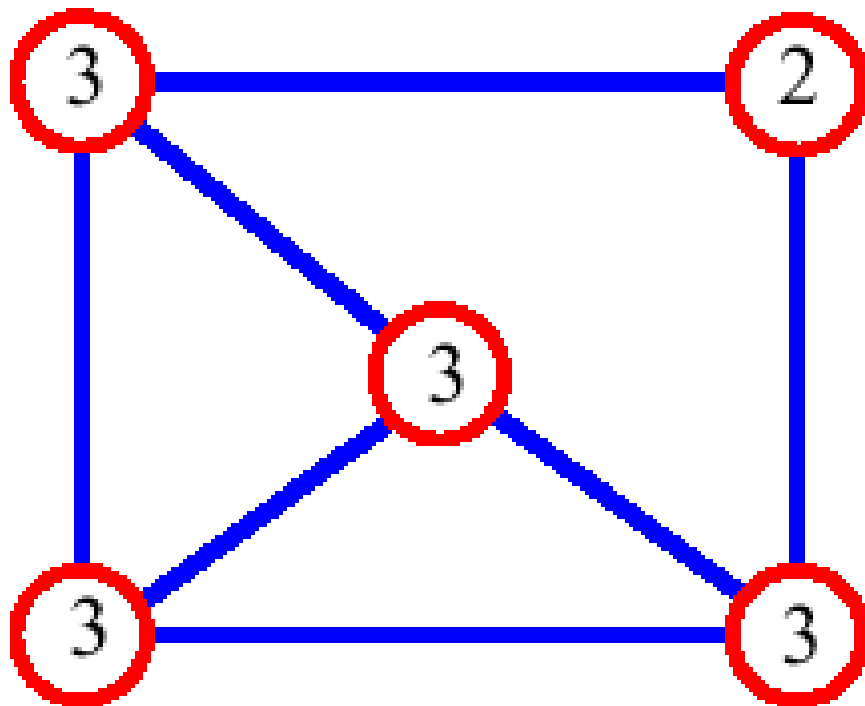
$\{(a, b), (a, c), (a, d),$   
 $(b, e), (c, d), (c, e),$   
 $(d, e)\}$

# Graph Terminology

also called  
“neighbors”

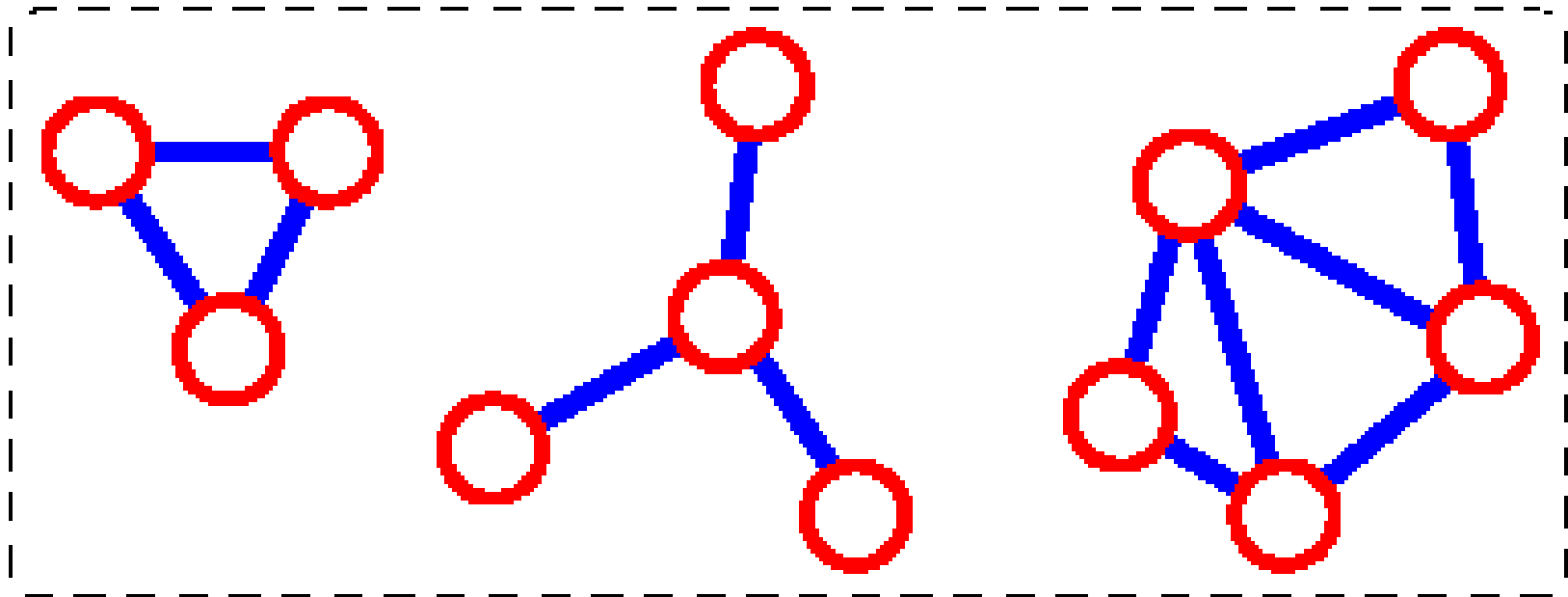
- **adjacent vertices**: connected by an edge
- **degree** (of a **vertex**): # of adjacent vertices

$$\sum_{v \in V} \deg(v) = 2(\# \text{ edges})$$



- Since adjacent vertices each count the adjoining edge, it will be counted twice

**connected component:** maximal connected subgraph. E.g., the graph below has 3 connected components.



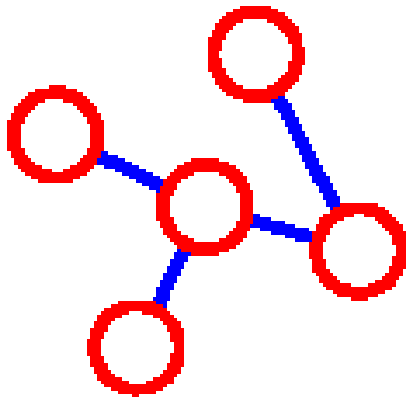
## More Connectivity

**n** = #vertices

**m** = #edges

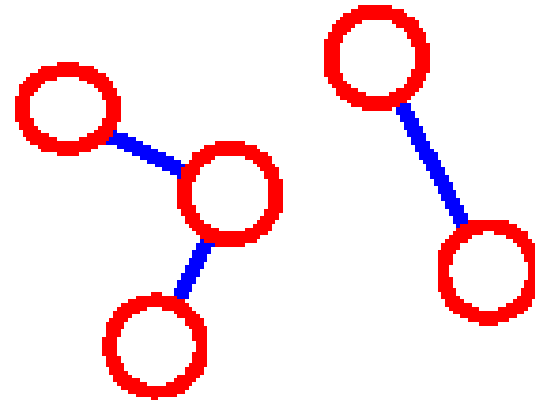
For a tree **m** = **n** - 1

A necessary but not sufficient condition for a graph to be a tree.



**n** = 5  
**m** = 4

If **m** < **n** - 1, G is not connected



**n** = 5  
**m** = 3

# We represent vertices using a collection of objects

- ▶ Each Vertex object contains information about itself
- ▶ Examples:
  - City name
  - IP address
  - People in a social network

# There are many options for representing edges of a graph

- ▶ Adjacency matrix
- ▶ Adjacency list. Each vertex stores...
  - pointers to other vertices?
  - named vertices using a `HashMap<Name,Vertex>`
  - An index into an array of the Vertex objects In each case, we need a way to store the vertex collection
- ▶ Edge list

To consider:

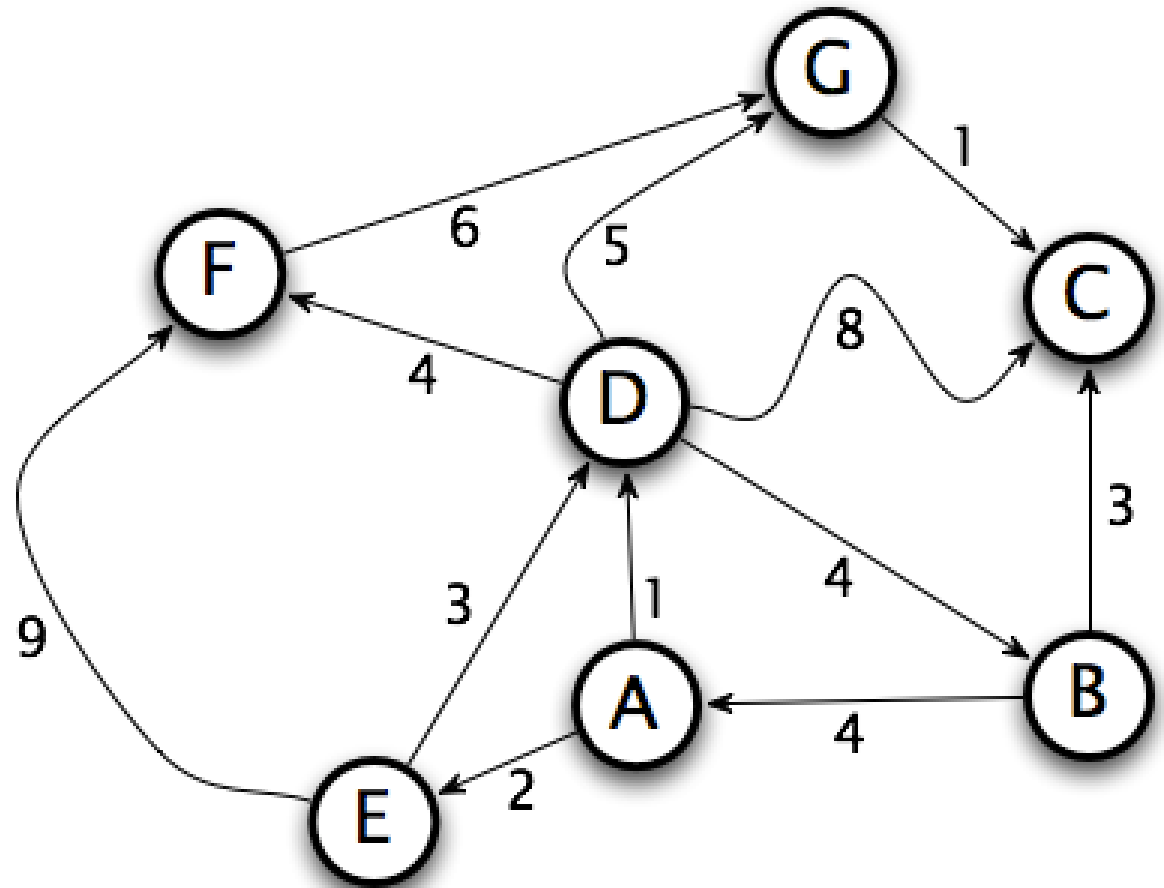
Why not just use a triangular “matrix”?

Does a boolean adjacency matrix make sense?



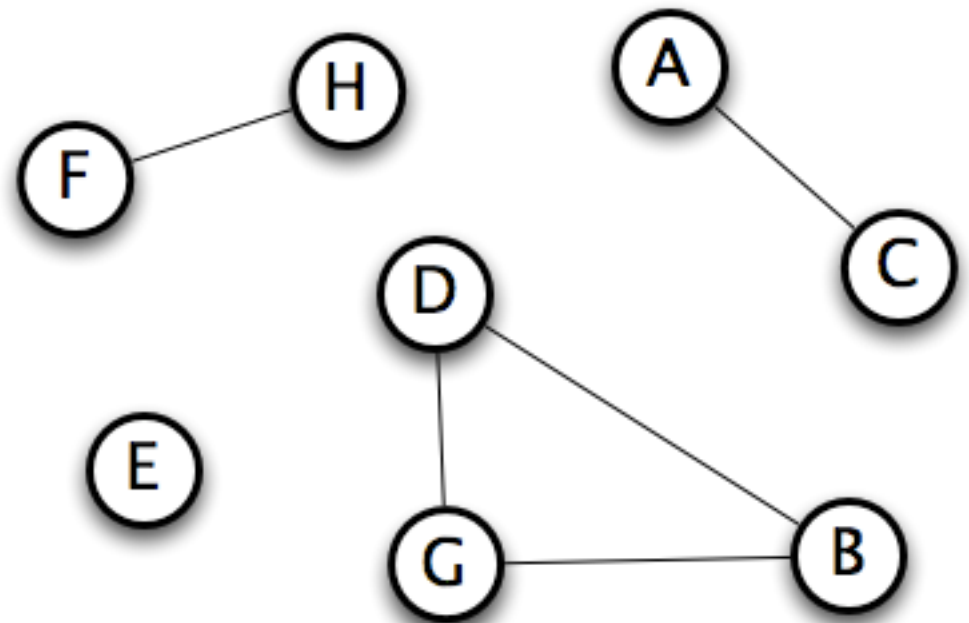
# Sample graph problem: Weighted Shortest Path

- ▶ What's the cost of the shortest path from A to each of the other nodes in the graph?



For much more on graphs, take MA/CSSE 473 or MA 477

- ▶ What's the size of the largest connected component?



Check out from SVN:  
RandomGraphs