## **CSSE 230 Day 25**

Skip Lists

### Reminders/Announcements

Complete the EditorTrees partner evaluation by Thursday

# Skip Lists

An alternative to balanced trees

### An alternative to AVL trees

- Indexed lists.
  - One–level index.
  - 2nd-level index.
  - 3rd-level index
  - log-n-level index.
- Problem: insertion and deletion.

Remember the problem with keeping trees completely balanced"?

- Solution: Randomized node height: Skip lists.
  - Pugh, 1990 CACM.
- http://iamwww.unibe.ch/~wenger/DA/SkipList/



Notice that skip lists do not share with binary trees the problem that threads are designed to solve.

# A slightly different skip list representation

- Uses a bit more space, makes the code simpler.
- Michael Goodrich and Roberto Tamassia.

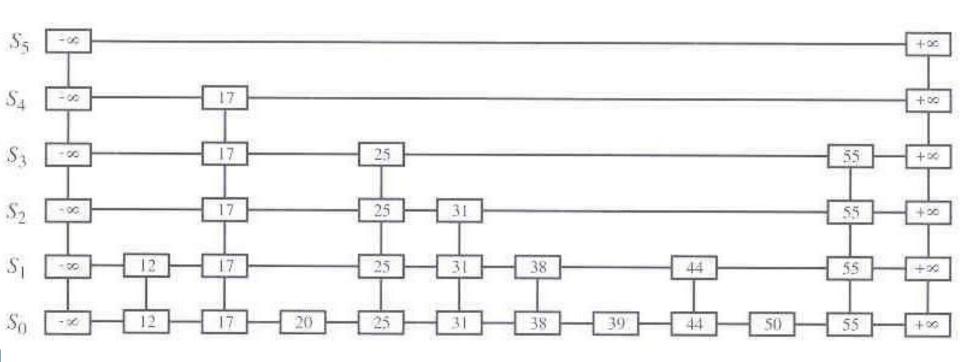


Figure 8.9: Example of a skip list.

### Methods in SkipListNode class

```
after(p): Return the position following p on the same level.
before(p): Return the position preceding p on the same level.
below(p): Return the position below p in the same tower.
above(p): Return the position above p in the same tower.
```

#### Search algorithm

- If S.below(p) is null, then the search terminates—we are at the bottom and have located the largest item in S with key less than or equal to the search key k. Otherwise, we drop down to the next lower level in the present tower by setting p ← S.below(p).
- 2. Starting at position p, we move p forward until it is at the right-most position on the present level such that key(p) ≤ k. We call this the scan forward step. Note that such a position always exists, since each level contains the special keys +∞ and -∞. In fact, after we perform the scan forward for this level, p may remain where it started. In any case, we then repeat the previous step.

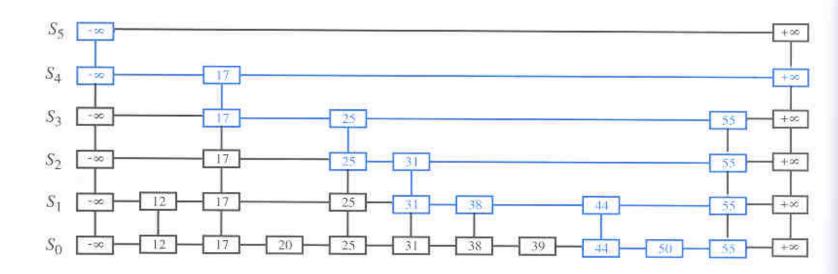
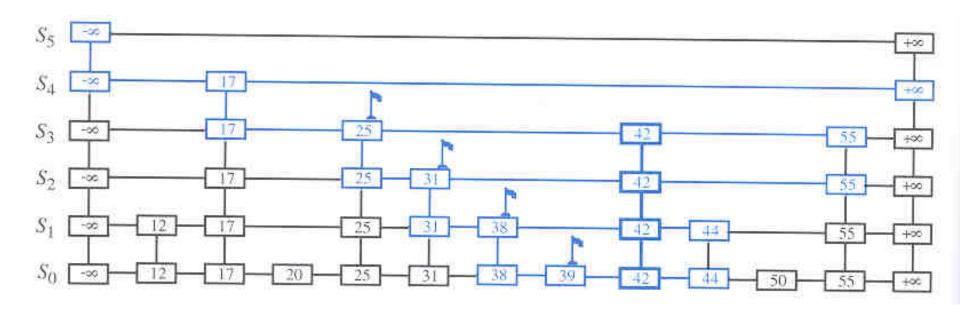
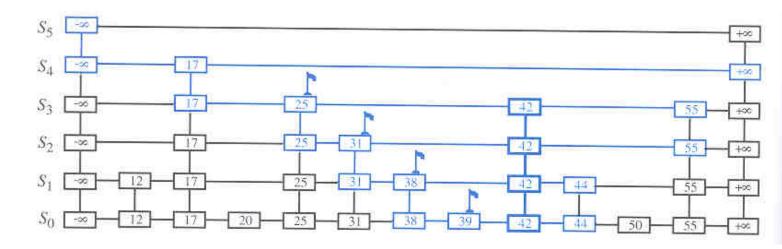


Figure 8.10: Example of a search in a skip list. The positions visited when searching for key 50 are highlighted in blue.

### Insertion diagram



### Insertion algorithm



```
Algorithm SkipInsert(k,e):

Input: Item (k,e)

Output: None

p \leftarrow \text{SkipSearch}(k)

q \leftarrow \text{insertAfterAbove}(p, \mathbf{null}, (k,e)) {we are at the bottom level}

while random() < 1/2 do

while above(p) = null do

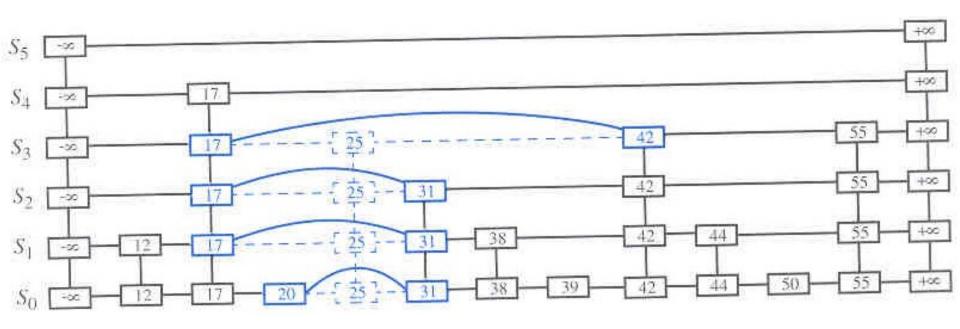
p \leftarrow \text{before}(p) {scan backward}

p \leftarrow \text{above}(p) {jump up to higher level}

q \leftarrow \text{insertAfterAbove}(p,q,(k,e)) {insert new item}
```

Code Fragment 8.5: Insertion in a skip list, assuming random() returns a random number between 0 and 1, and we never insert past the top level.

### Remove algorithm



### (sort of) Analysis of Skip Lists

- No guarantees that we won't get O(N) behavior.
  - The interaction of the RNG and the order in which things are inserted/deleted could lead to a long chain of nodes with the same height.
  - But this is very unlikely.
  - Expected time for search, insert, and remove are O(log n).