

Dimensional Analysis on Pipe Flow

Given a water pipe as follows:



If the pressure drop due to friction in the pipe is  $DP$  and it depends on the following fluid properties and geometry parameters:

- a. density of water,  $\rho$
- b. velocity of flow,  $V$
- c. diameter of pipe,  $D$
- d. surface roughness of pipe,  $e$
- e. dynamic viscosity of fluid,  $\mu$
- f. length of pipe,  $l$

so that

$$DP = f(\rho, V, D, e, \mu, l)$$

Perform a dimensional analysis on the above functional dependency by choosing the density of water, velocity of flow and diameter of pipe as the repeating variables.